

# Safety verification for deep neural networks with provable guarantees



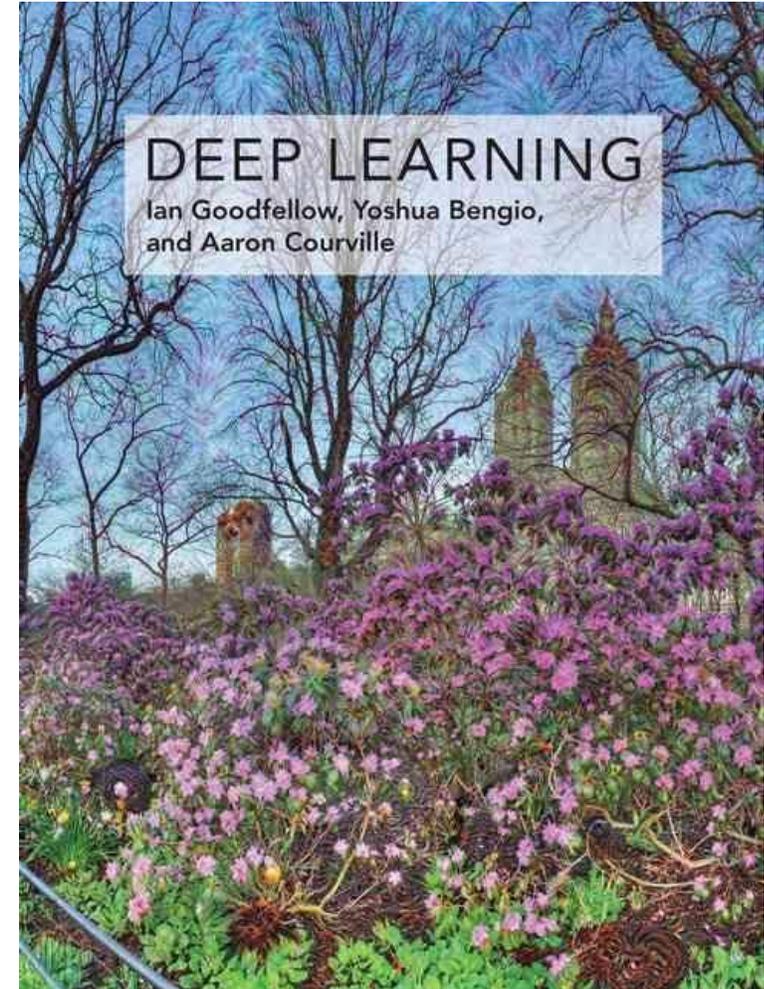
Prof. Marta Kwiatkowska

Department of Computer Science  
University of Oxford

# The unstoppable rise of deep learning

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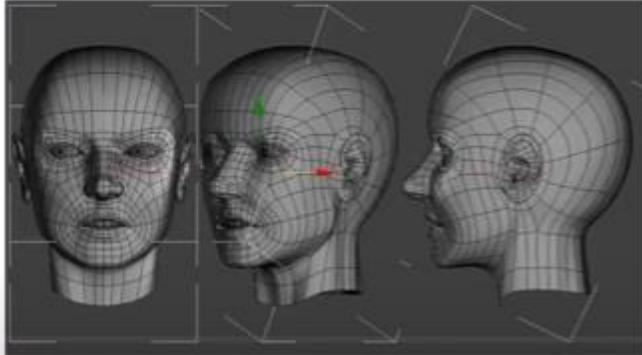
- **Neural networks timeline**
  - 1940s First proposed
  - 1998 Convolutional nets
  - 2006** Deep nets trained
  - 2011 Rectifier units
  - 2015 Vision breakthrough
  - 2016 Win at Go
  - 2019** Turing Award
- **Enabled by**
  - Big data
  - Flexible, easy to build models
  - Availability of GPUs
  - Efficient inference



# Deep learning with everything

## DeepFace

### Closing the Gap to Human-Level Performance in Face Verification



[Yaniv Taigman](#)  
[Ming Yang](#)  
[Marc'Aurelio Ranzato](#)  
[Lior Wolf](#)  
- 2014

97.35% accuracy  
Trained on the largest facial dataset - 4M facial images belonging to more than 4,000 identities.



Google Translate—here shown on a mobile phone—will use deep learning to improve its translations between texts.



Build for voice with Alexa

[Learn more](#)

amazon alexa

# Deep learning in healthcare

nature

International weekly journal of science

Home | News | Research | Careers & Jobs | Current Issue | Archive | Audio & Video | For Authors

Archive > Volume 542 > Issue 7639 > Letters > Article > Article metrics > News

## Article metrics for:

### Dermatologist-level classification of skin cancer with deep learning

Andre Esteva, Brett Kuprel, Roberto A. Novoa, Justin Ko, Susan M. Swetter, Helen M. Blau

*Nature* 542, 115–118 (02 February 2017) | doi:10.1038/nature21056

Last updated: 24 July 2017 10:10:28 EDT

The Stanford University team said the findings were "incredibly exciting" and will now be tested in clinics.

Eventually, they believe using AI could revolutionise healthcare by turning any smartphone into a cancer scanner.

Cancer Research UK said it could become a useful tool for doctors.

The AI was repurposed from software developed by Google that had learned to spot the difference **between images of cats and dogs**.

## LETTER

<https://doi.org/10.1038/s41586-019-1019-1>

### A clinically applicable approach to continuous prediction of future acute kidney injury

Nenad Tomašev<sup>1\*</sup>, Xavier Glorot<sup>1</sup>, Jack W. Rae<sup>1,2</sup>, Michal Zielinski<sup>1</sup>, Harry Askham<sup>1</sup>, Andre Saraiva<sup>1</sup>, Anne Mottram<sup>1</sup>, Clemens Meyer<sup>1</sup>, Suman Ravuri<sup>1</sup>, Ivan Protsyuk<sup>1</sup>, Alistair Connell<sup>1</sup>, Cian O. Hughes<sup>1</sup>, Alan Karthikesalingam<sup>1</sup>, Julien Cornebise<sup>1,12</sup>, Hugh Montgomery<sup>3</sup>, Geraint Rees<sup>4</sup>, Chris Laing<sup>5</sup>, Clifton R. Baker<sup>6</sup>, Kelly Peterson<sup>7,8</sup>, Ruth Reeves<sup>9</sup>, Demis Hassabis<sup>1</sup>, Dominic King<sup>1</sup>, Mustafa Suleyman<sup>1</sup>, Trevor Back<sup>1,13</sup>, Christopher Nielson<sup>10,11,13</sup>, Joseph R. Ledsam<sup>1,13\*</sup> & Shakir Mohamed<sup>1,13</sup>

The early prediction of deterioration could have an important role in supporting healthcare professionals, as an estimated 11% of deaths in hospital follow a failure to promptly recognize and treat deteriorating patients<sup>1</sup>. To achieve this goal requires predictions

Promising recent work on modelling adverse events from electronic health records<sup>2–17</sup> suggests that the incorporation of machine learning may enable the early prediction of AKI. Existing examples of sequential AKI risk models have either not demonstrated a clinically applicable

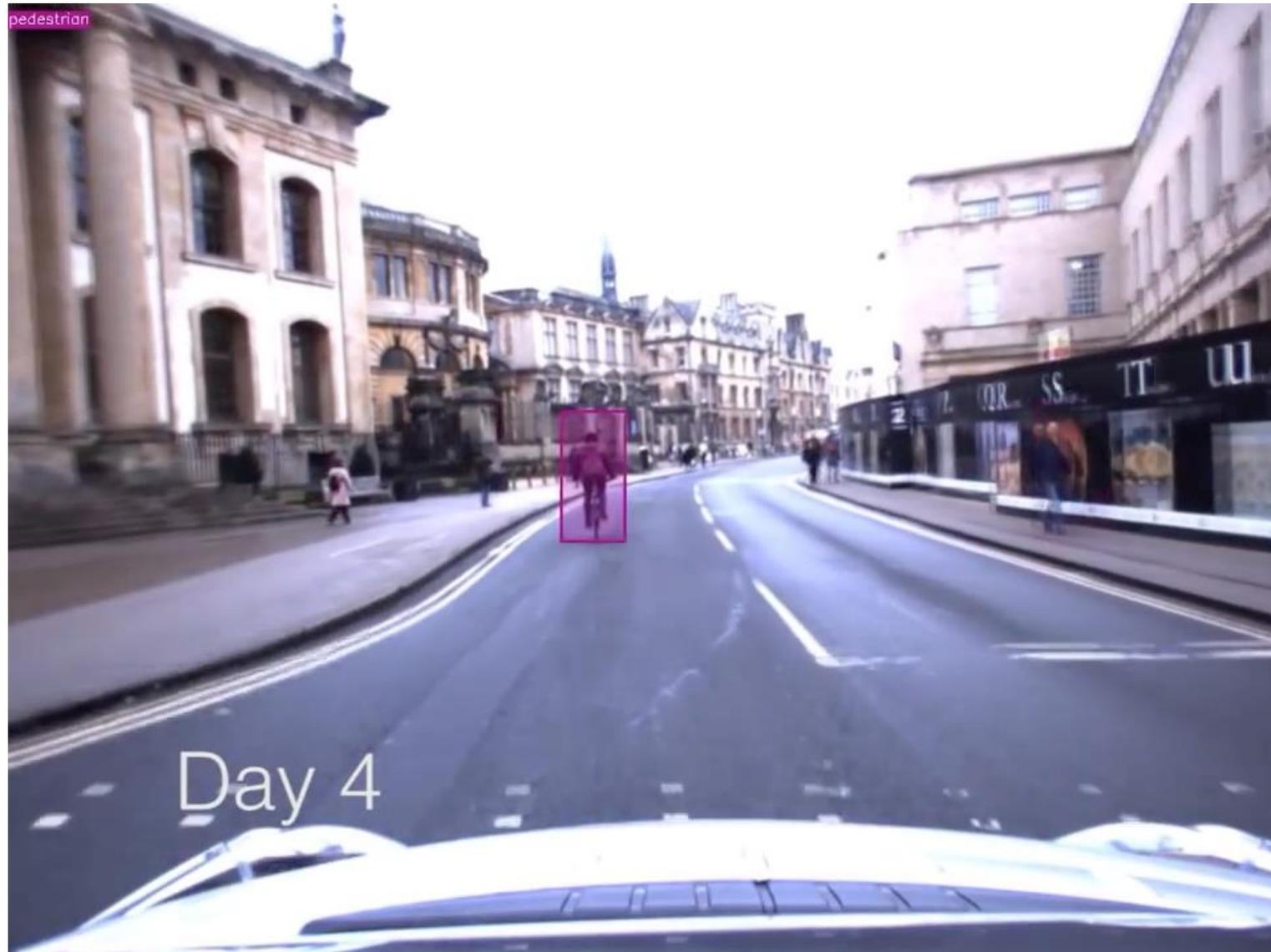
# Much excitement about self-driving

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RUSH HOUR

# Self-driving in Oxford....



# Would you trust a self-driving car?

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We're looking to learn from people with diverse transportation needs. Here are some of the first riders who are already using our self-driving cars every day.



## Ted and Candace

A typical day in Ted and Candace's household is full of busy activities across both the parents and their four children: Abbi, Brielle, Izzy and Trey. This lively family is now using our self-driving cars to get to work, shuttle four kids to school and juggle everything from the parents' weekly date night to their children's soccer practice. They are excited about giving everyone in their home a greater sense of freedom and independence.

Waymo early riders, Tesla, Uber, ...

In the UK FiveAI, Oxbotica, ...

# Unwelcome news recently...

## *Self-Driving Uber Car Kills Pedestrian in Arizona, Where Robots Roam*

Leer en español

By DAISUKE WAKABAYASHI MARCH 19, 2018

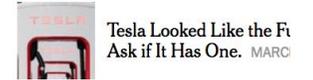


## *Tesla Says Crashed Vehicle Had Been on Autopilot Before Fatal Accident*

By GREGORY SCHMIDT MARCH 31, 2018



RELATED COVERAGE



***Fatal Tesla Crash Raises New Questions About Autopilot System***

***U.S. Safety Agency Criticizes Tesla Crash Data Release***

**How can this happen if we have 99.9% accuracy?**

# An AI safety problem...

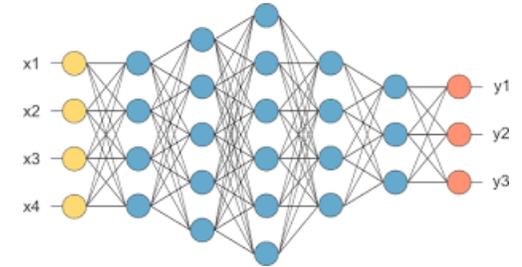
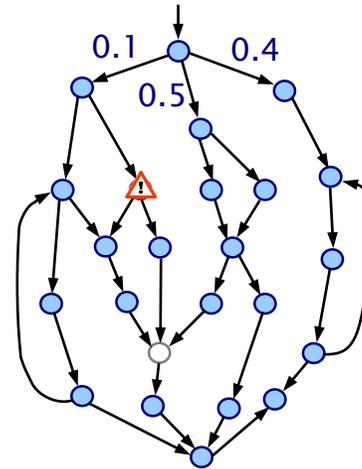
- Complex scenarios
  - goals
  - perception
  - **autonomy**
  - situation awareness
  - context (social, regulatory)
  - **trust**
  - ethics
- **Safety-critical**, so guarantees needed
- Should failure occur, **accountability** needs to be established



Credit: Anita Dufala/Public source

# Modelling challenges

- Cyber-physical systems
  - **hybrid** combination of continuous and discrete dynamics, with stochasticity
  - **autonomous** control
- Data rich, data-enabled models
  - achieved through **learning**
  - parameter **estimation**
  - continuous **adaptation**
- Heterogeneous components, including learning based
  - model-based design
  - automated verification via **model checking**
  - **correct-by-construction model synthesis** from specifications



# Probabilistic verification and synthesis

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- **Stochasticity** ever present
  - randomisation, uncertainty, risk
- Need **quantitative, probabilistic** guarantees for:
  - safety, security, reliability, performance, resource usage, trust, authentication, ...
- **Examples**
  - (**reliability**) “the probability of the car crashing in the next hour is less than 0.001”
  - (**energy**) “energy usage is below 2000 mA per minute”
- My focus is on automated, tool-supported methodologies
  - probabilistic model checker **PRISM**, [www.prismmodelchecker.org](http://www.prismmodelchecker.org)
  - HVC 2016 Award (joint with Dave Parker and Gethin Norman)
- Applied to a wide range of systems...



# OK, but what is probabilistic verification good for?

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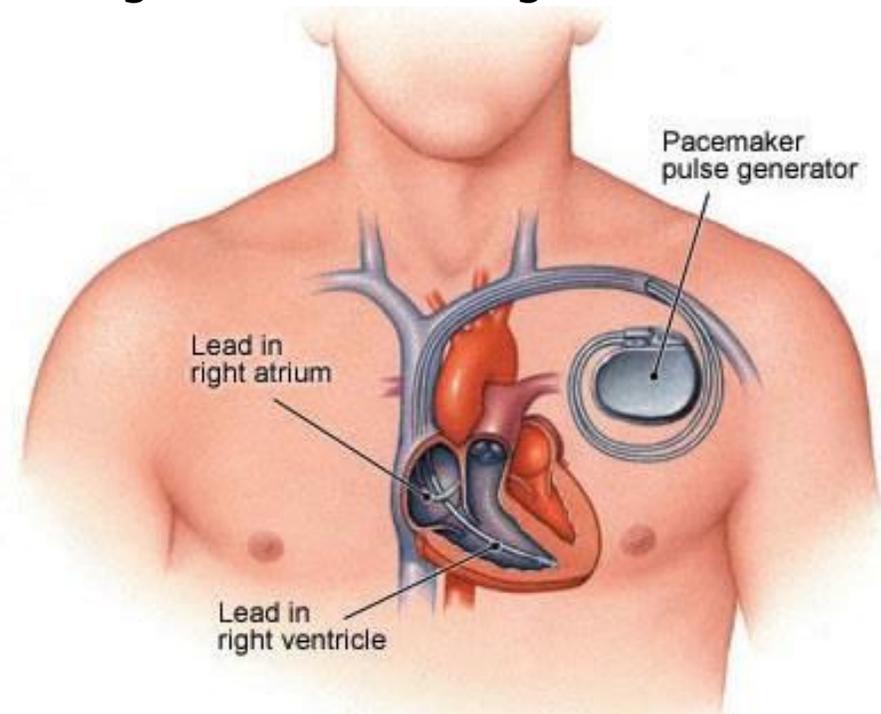


ALL RIGHT, BUT APART FROM  
THE SANITATION,  
THE MEDICINE,  
EDUCATION, WINE,  
PUBLIC ORDER,  
IRRIGATION, ROADS,  
THE FRESH-WATER SYSTEM,  
AND PUBLIC HEALTH,  
WHAT HAVE THE ROMANS EVER DONE FOR US?

# Case study: Cardiac pacemaker

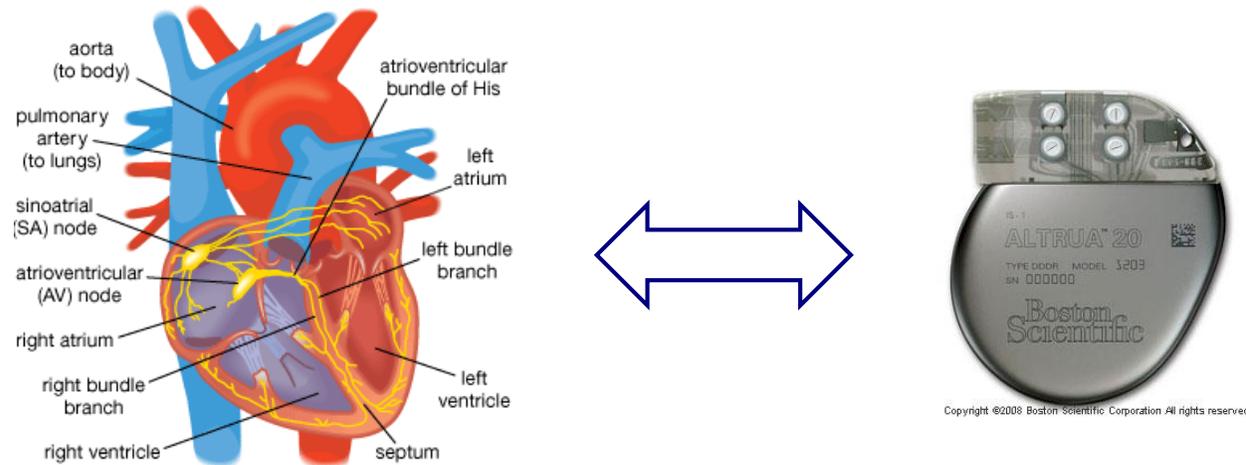
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- How it works
  - **reads** electrical signals through sensors in the right atrium and right ventricle
  - monitors the **timing** of heart beats and local electrical activity
  - generates **artificial** pacing signal as necessary
- Safety-critical **real-time** system!
- The guarantee
  - (**basic safety**) maintain 60–100 beats per minute
- **Killed by code**: FDA recalls 23 defective pacemaker devices because of adverse health consequences or death, six likely caused by software defects (2010)

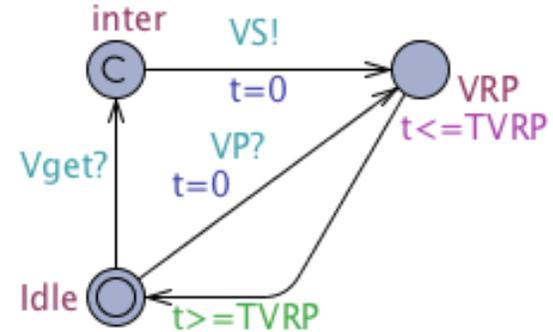
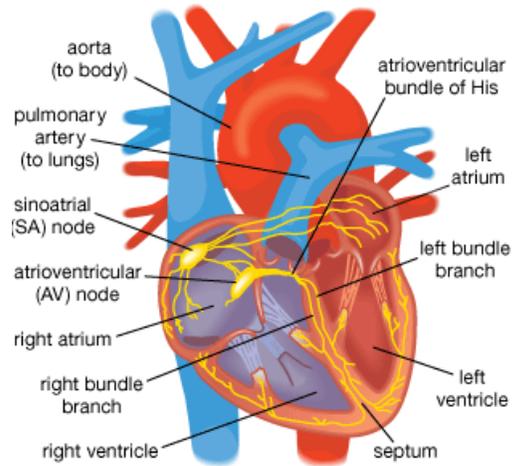


# Modelling framework

Model the pacemaker and the heart, compose and verify



# Modelling framework



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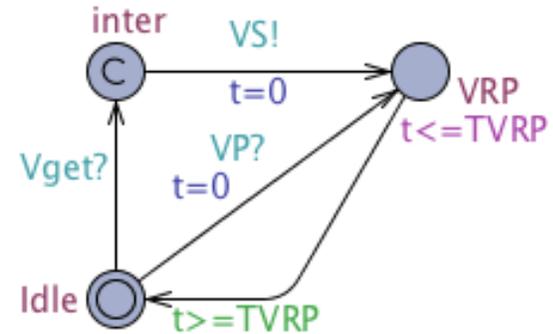
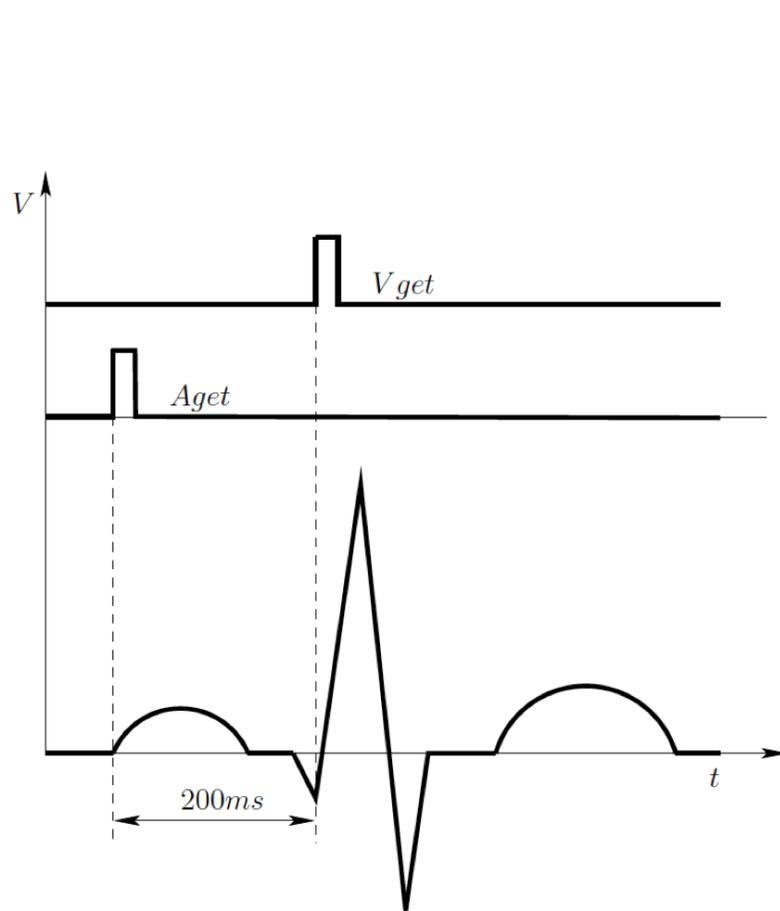
module VRP

s_vrp: [0..2] init 0;
t_vrp : clock;

// Invariants for clock t_vrp
invariant
    (s_vrp = 2 => (t_vrp <= TVRP)) &
    (s_vrp = 1 => (t_vrp <= 0 ))
endinvariant

[Vget] (s_vrp = 0) -> (s_vrp' = 1) & (t_vrp' = 0);
[VP]   (s_vrp = 0) -> (s_vrp' = 2) & (t_vrp' = 0);
    
```

# Modelling framework



```

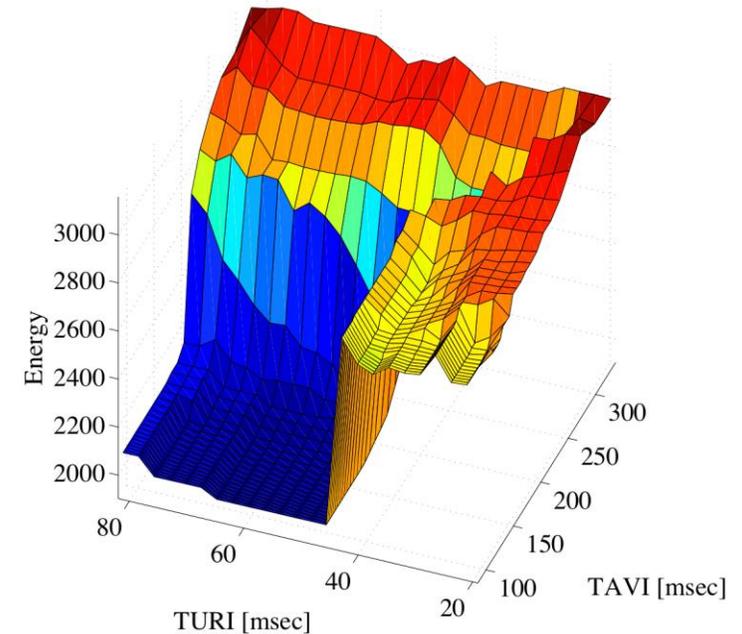
module VRP
s_vrp: [0..2] init 0;
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// Invariants for clock t_vrp
invariant
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    (s_vrp = 1 => (t_vrp <= 0 ))
endinvariant

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[VP]   (s_vrp = 0) -> (s_vrp' = 2) & (t_vrp' = 0);
    
```

# Pacemaker verification

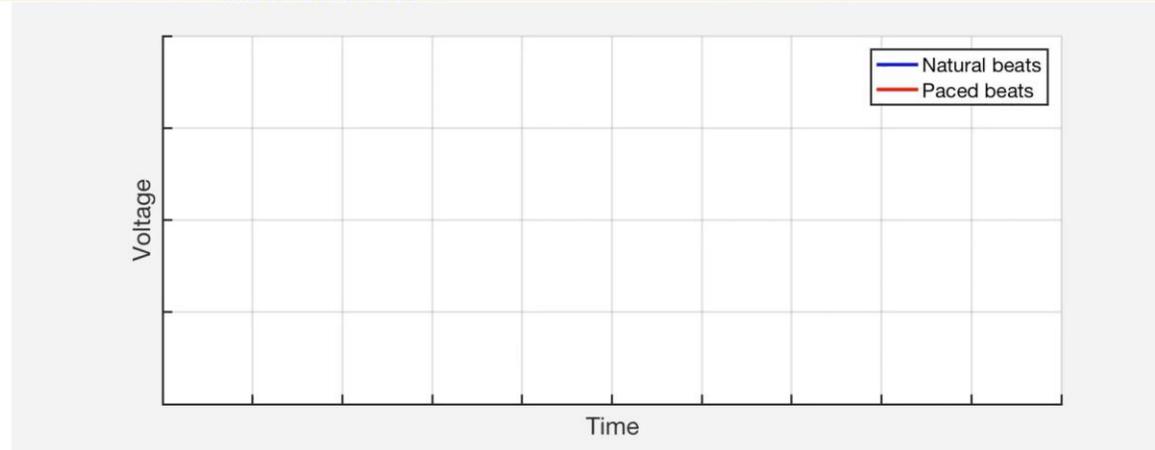
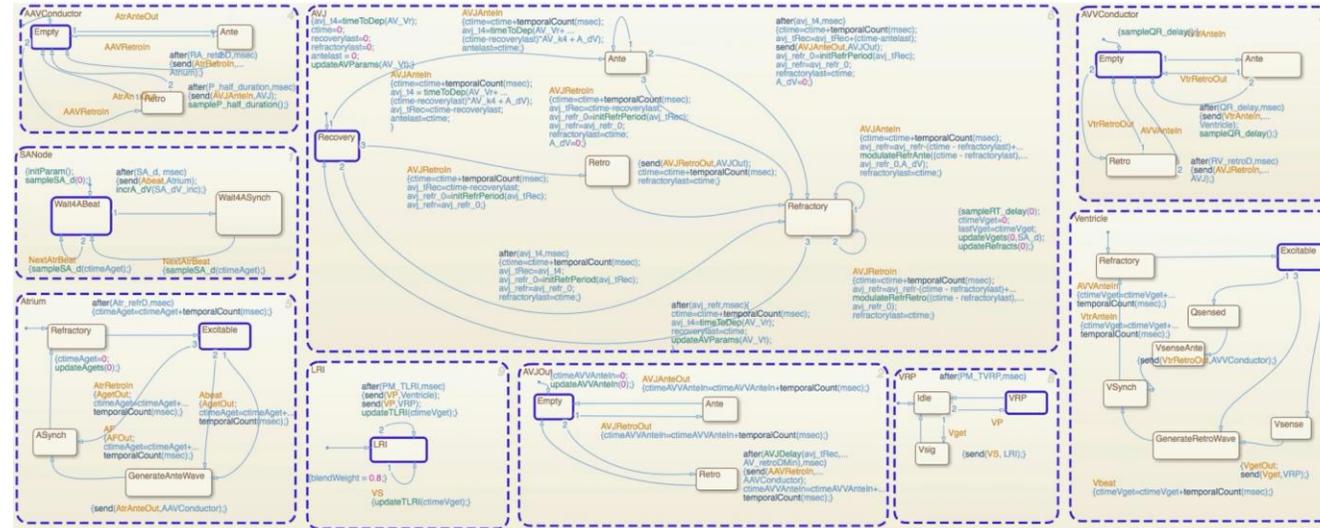
- Basic guarantees
  - (**basic safety**) maintain 60–100 beats per minute
  - (**energy usage**) detailed analysis, plotted against timing parameters of the pacemaker
- Advanced guarantees
  - rate-adaptive pacemaker, for patients with chronotropic deficiency
  - (**advanced safety**) adapt the rate to exercise and stress levels
  - **in silico** testing





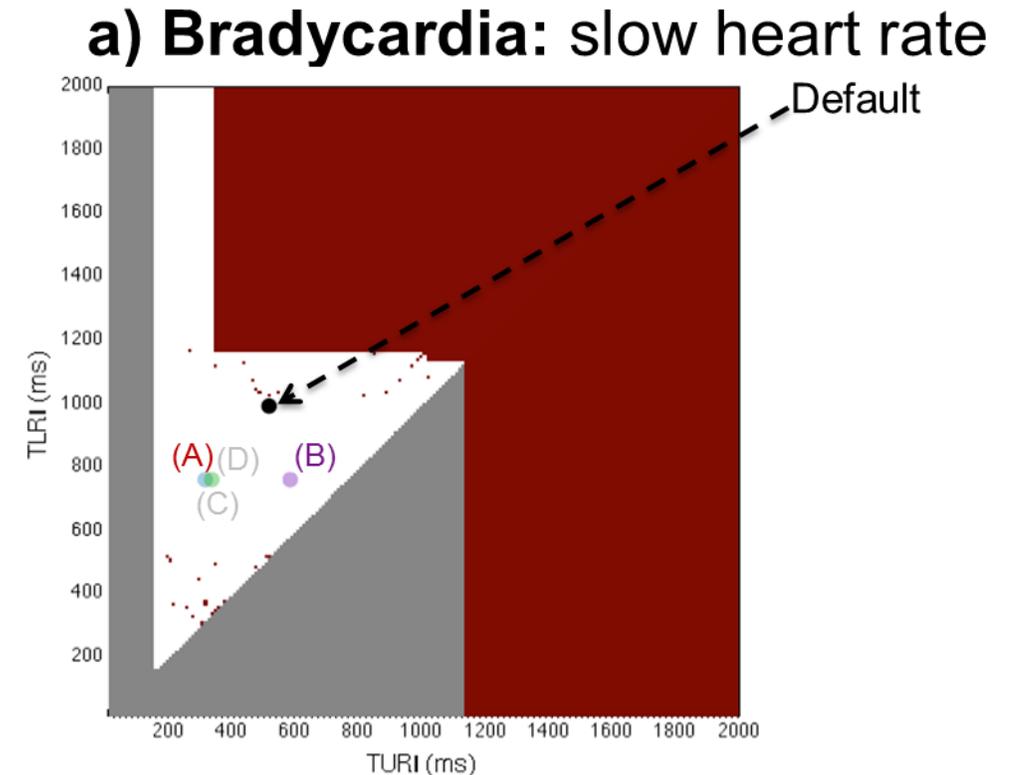


# Bradycardia heart, paced

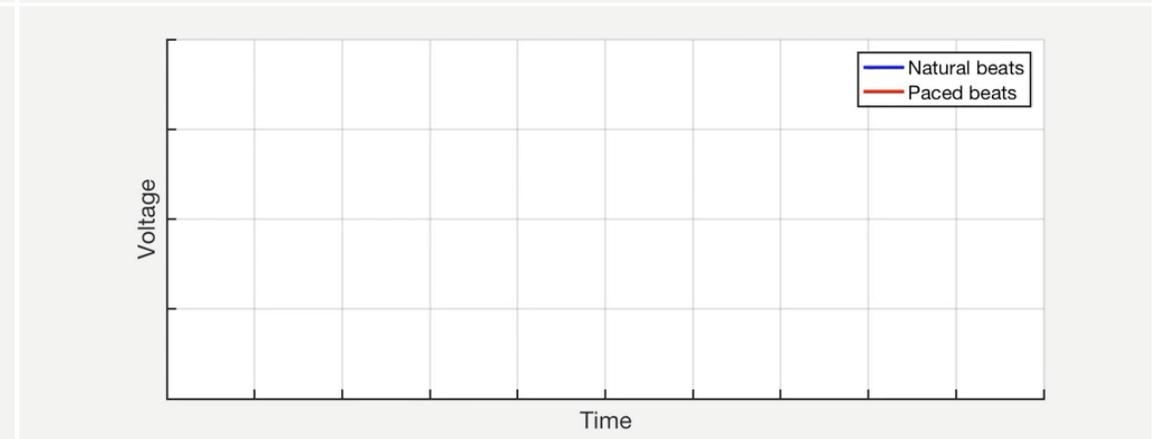
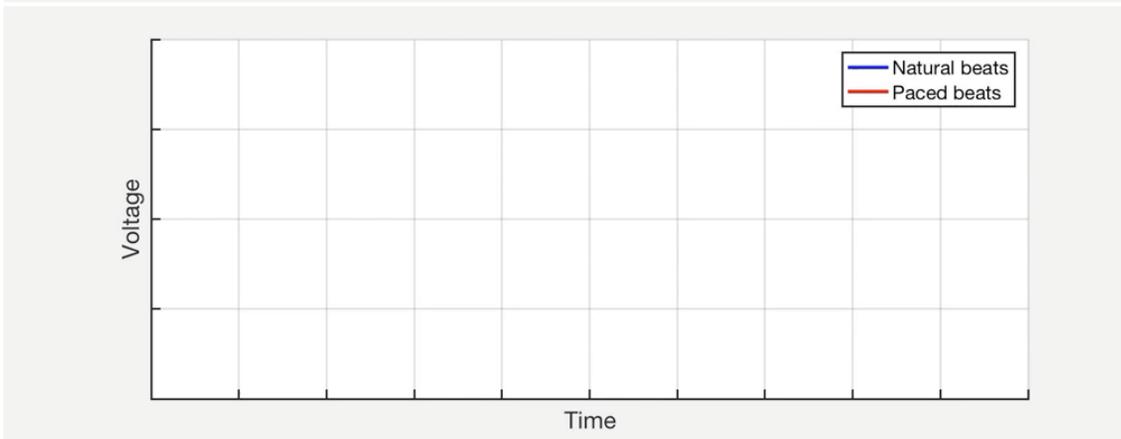
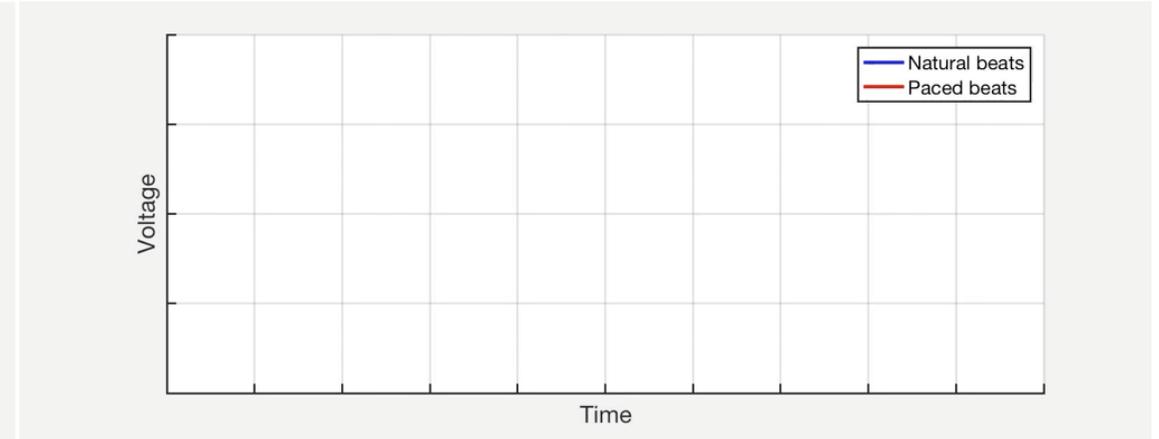
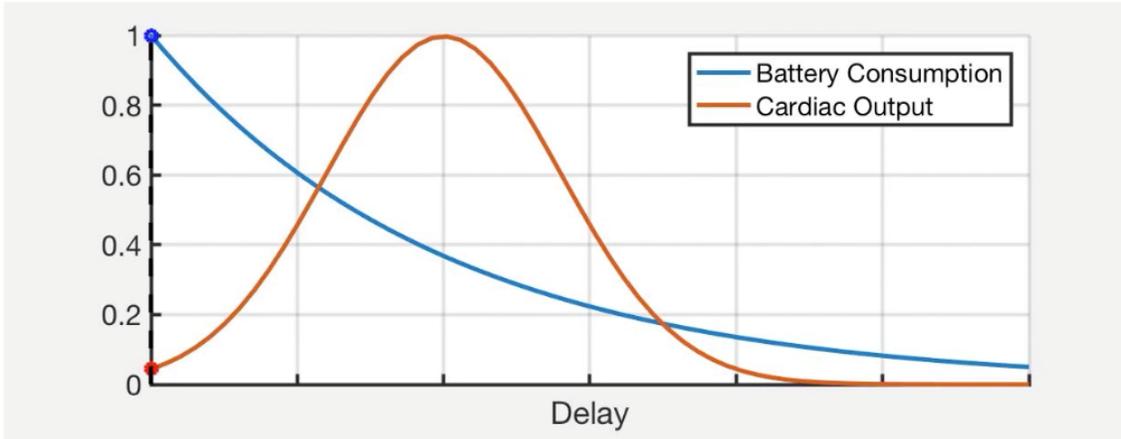


# Parameter synthesis for pacemakers

- Can we adapt the pacing rate to patient's ECG to
  - minimise energy usage?
  - maximise cardiac output?
  - explore trade offs?
- The guarantee
  - (**optimal timing delay synthesis**): find values for timing delays that optimise a given objective, adapted to patient's ECG
- Significant improvement over default values



# Trade offs in optimal delay synthesis



# Case study: ECG biometrics

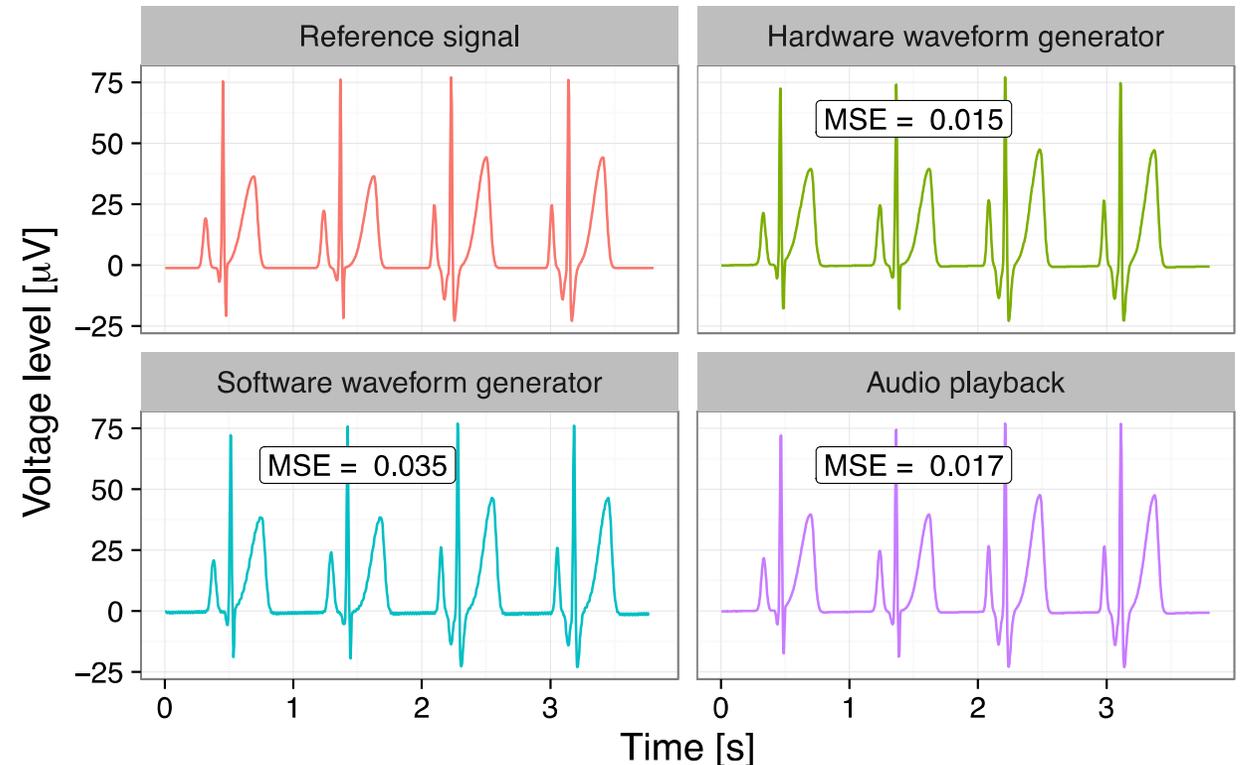
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- Biometrics increasing in popularity
  - are they secure?
- Nymi band
  - ECG used as a **biometric identifier**
  - biometric template created first
  - compared with real ECG signal
- Proposed uses
  - for access into buildings and restricted spaces
  - for payment
  - etc



# Attack on ECG biometrics

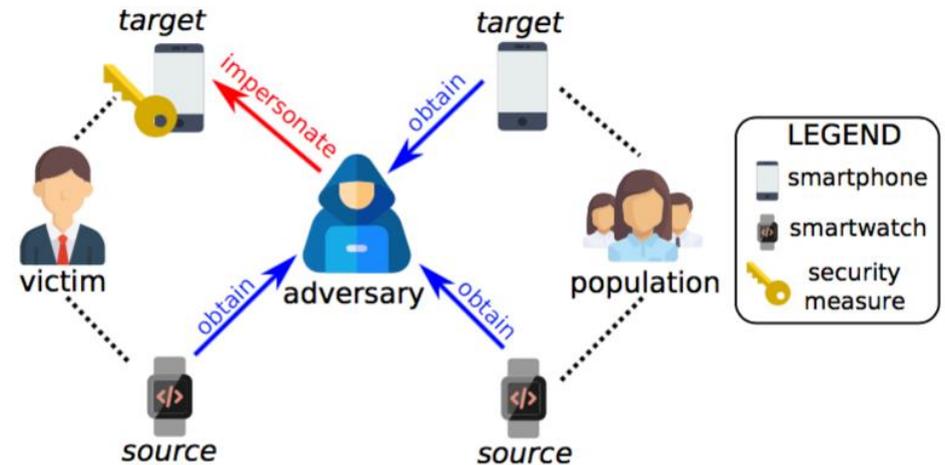
- We use synthetic ECGs to **impersonate** a user
  - build model from data, 41 volunteers
  - inject synthetic signals to break authentication
  - 80% success rate
- **Results**
  - serious **weakness**
  - countermeasures needed



- Modelling essential, good for **attacks**...

# Case study: Transferability of attack

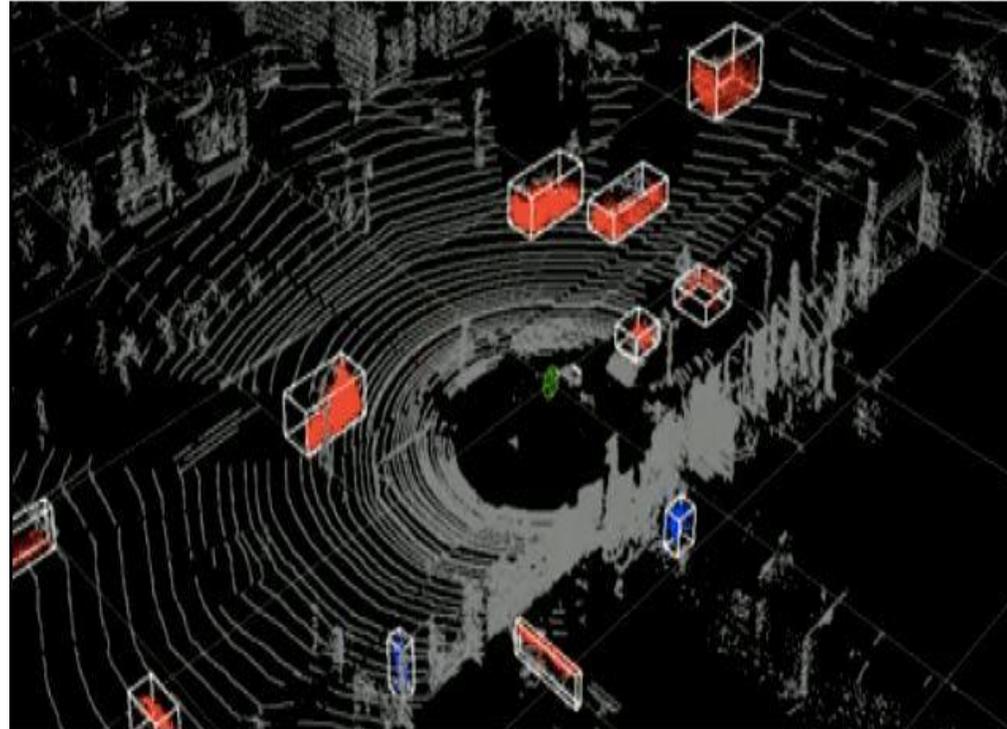
- Beware your **fitness tracker!**
- How easy it is to **predict** attacks when collecting data from **different** sources
  - ECG
  - eye movements
  - mouse movements
  - touchscreen dynamics
  - gait
  - etc
- **Human study**
  - easy for eye movements
  - ECG more chaotic



# Back to the challenge of autonomous driving...

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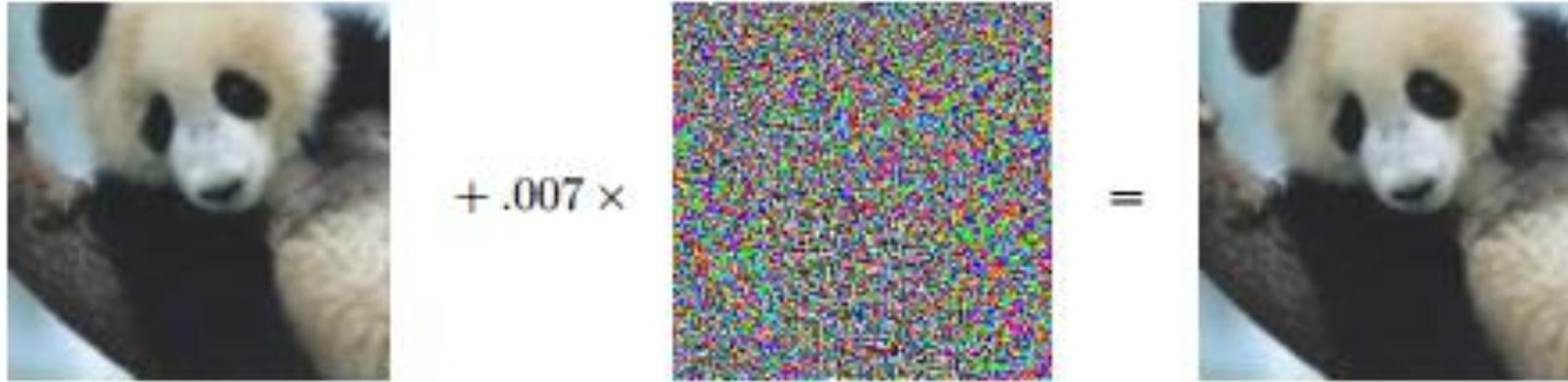
- Things that can go wrong in perception software
  - sensor failure
  - object detection failure
- Machine learning software
  - not clear how it works
  - does **not** offer guarantees
- Yet **safety-critical** applications



Lidar image, Credit: Oxford Robotics Institute

# Deep neural networks can be fooled!

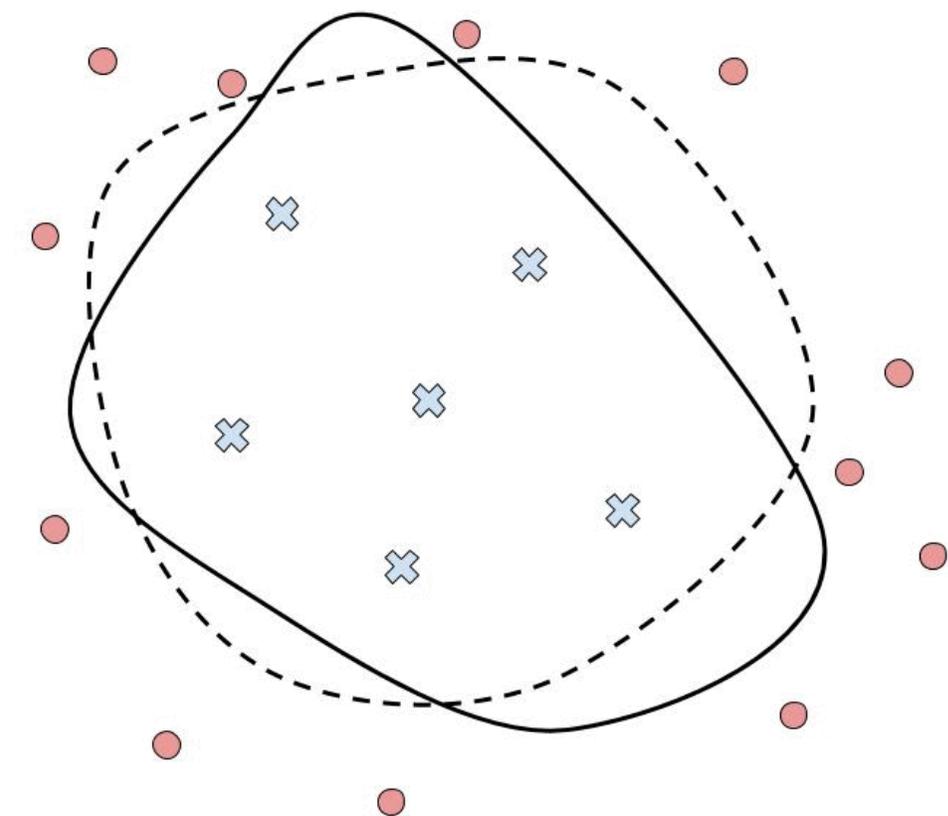
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- They are unstable wrt **adversarial perturbations**
  - often imperceptible changes to the image [Szegedy et al 2014, Biggio et al 2013 ...]
  - sometimes artificial white noise
  - practical attacks, potential security risk
  - transferable between different architectures
  - not just image classification: also images segmentation, pose recognition, sentiment analysis...

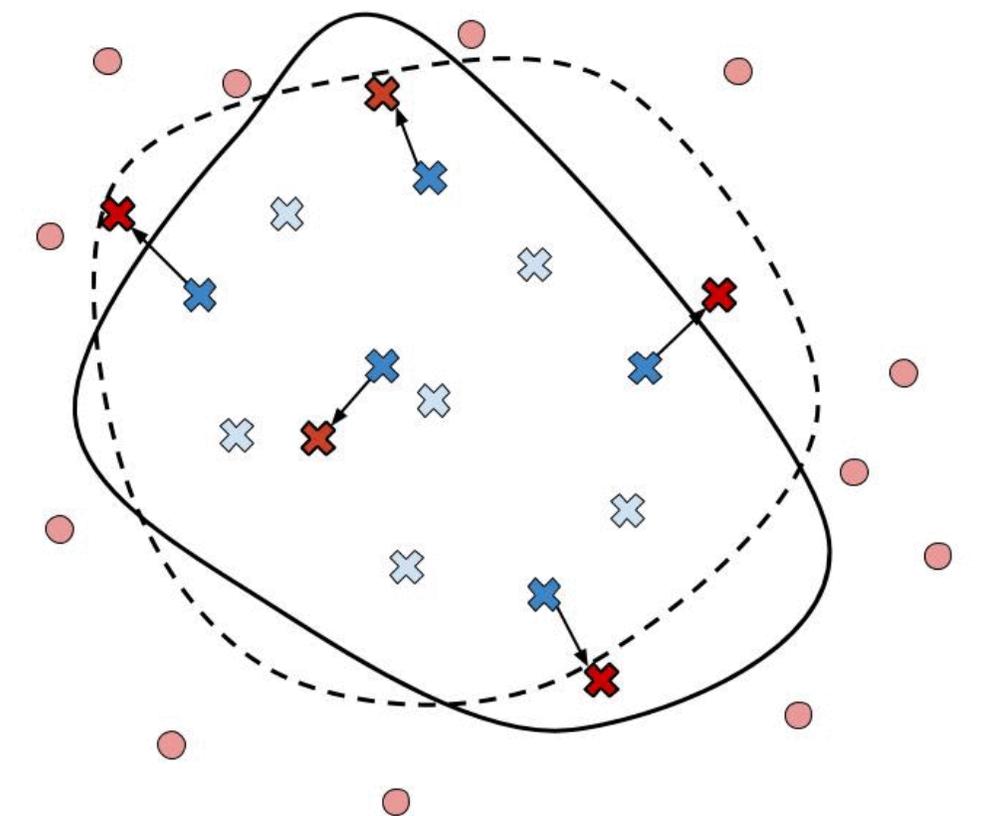
# Training vs testing

## Model training



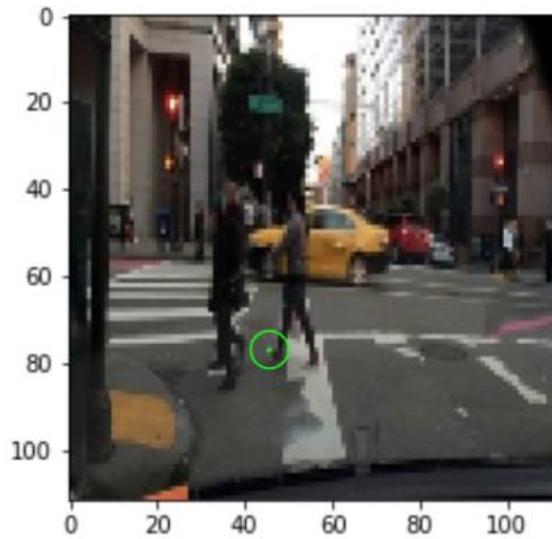
--- Task decision boundary  
— Model decision boundary  
⊗ Training points for class 1  
● Training points for class 2

## Model testing



--- Task decision boundary  
— Model decision boundary  
⊗ Training points for class 1  
● Training points for class 2  
⊗ Testing points for class 1  
⊗ Adversarial examples for class 1

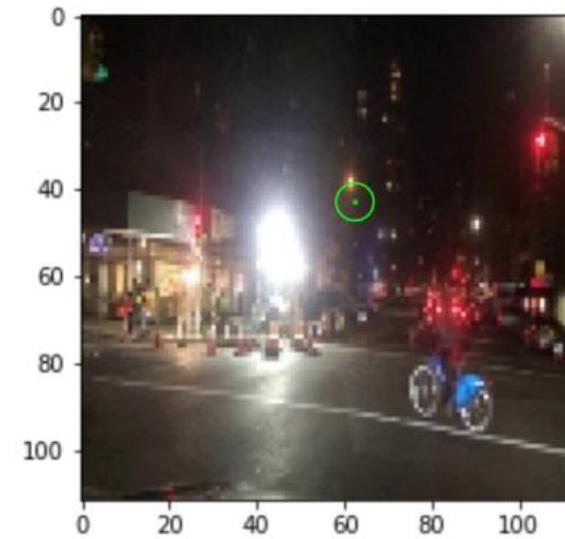
# Should we worry about safety of self-driving?



(a)



(b)

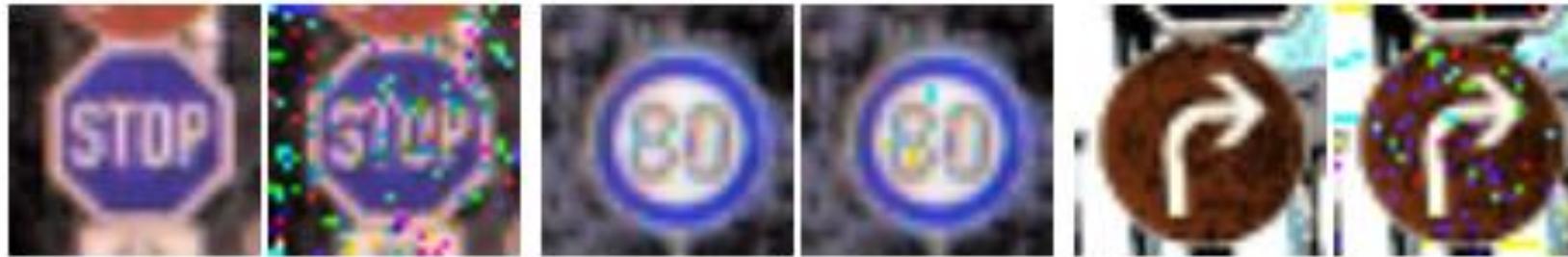


(c)

- Deep neural networks are unstable wrt **adversarial perturbations**
  - Nexar Traffic Light Challenge: **red light** classified as **green** with 68%/95%/78% confidence after one pixel change

# German traffic sign benchmark...

---



stop

30m  
speed  
limit

80m  
speed  
limit

30m  
speed  
limit

go  
right

go  
straight

Confidence 0.999964

0.99

# Aren't these artificial?

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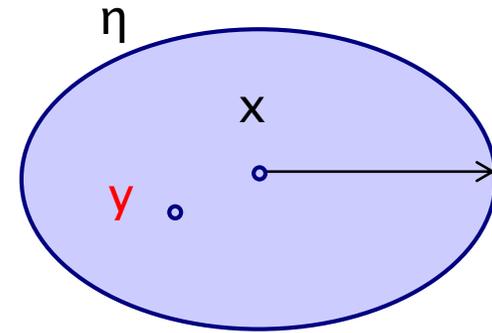
Real traffic signs in Alaska!

Need to consider **physical** attacks, not only digital...

# Safety of classification decisions

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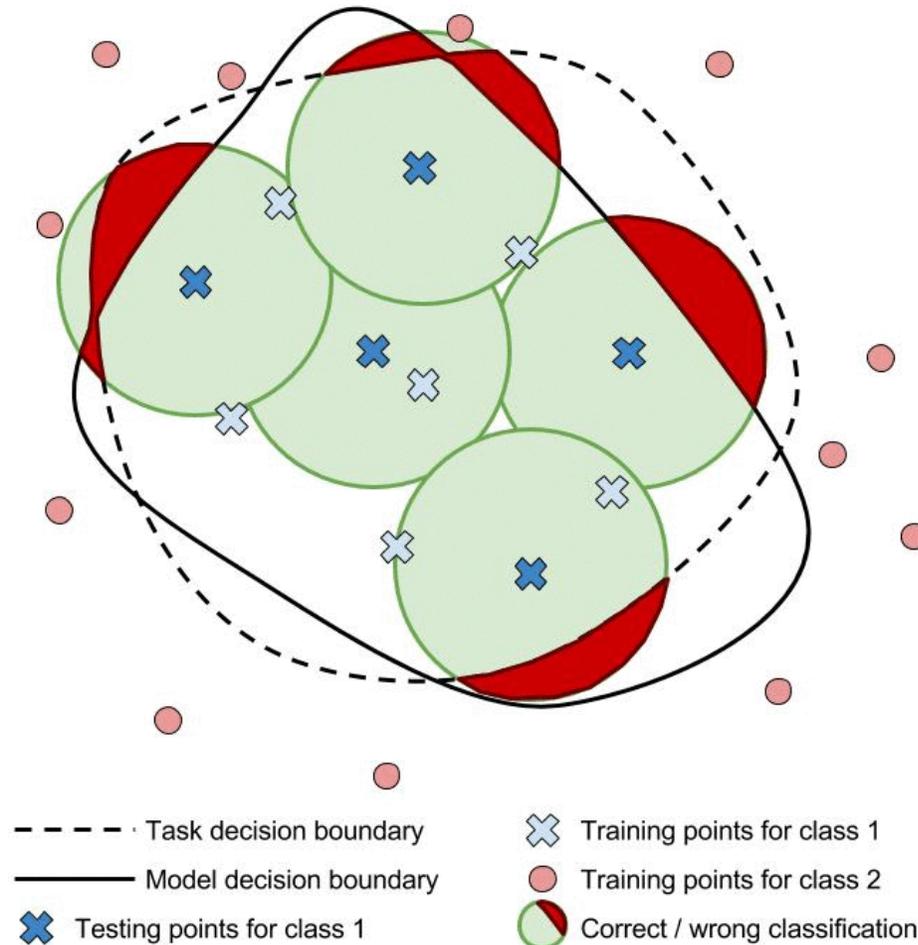
- Safety assurance process is complex
- Here focus on **safety at a point** as part of such a process
  - same as pointwise robustness...
- Assume given
  - trained network  $f : D \rightarrow \{c_1, \dots, c_k\}$
  - diameter for support region  $\eta$
  - norm, e.g.  $L^2, L^\infty$
- Define safety as **invariance** of classification decision over  $\eta$ 
  - i.e.  $\nexists y \in \eta$  such that  $f(x) \neq f(y)$
- Also wrt family of safe **manipulations**
  - e.g. scratches, weather conditions, camera angle, etc



# Training vs testing vs verification

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## Model verification



# Searching for adversarial examples...

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- Input space for most neural networks is high dimensional and non-linear
- Where do we start?
- How can we apply **structure** to the problem?

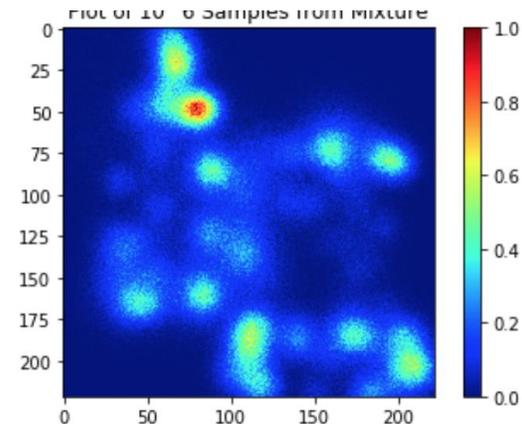
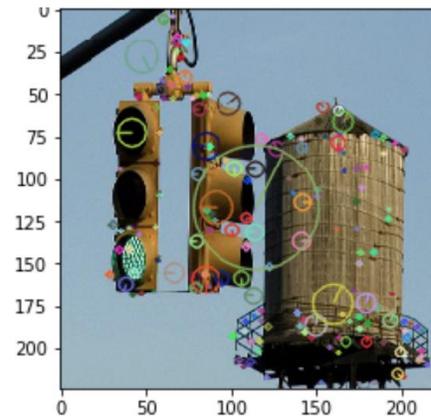


- Image of a tree has  $4,000 \times 2,000 \times 3$  dimensions = 24,000,000 dimensions
- We would like to find a very 'small' change to these dimensions

# Feature-based representation

- Employ the SIFT algorithm to extract features
- Reduce dimensionality by focusing on **salient features**
- Use a Gaussian mixture model in order to assign each pixel a probability based on its **perceived saliency**

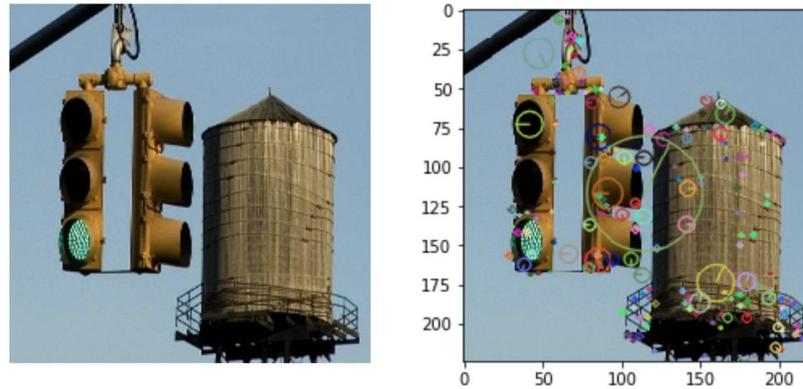
$$G_{i,x} = \frac{1}{\sqrt{2\pi\lambda_{i,s}^2}} \exp\left(\frac{-(p_x - \lambda_{i,x})^2}{2\lambda_{i,s}^2}\right) \quad G_{i,y} = \frac{1}{\sqrt{2\pi\lambda_{i,s}^2}} \exp\left(\frac{-(p_y - \lambda_{i,y})^2}{2\lambda_{i,s}^2}\right)$$



# Game-based search

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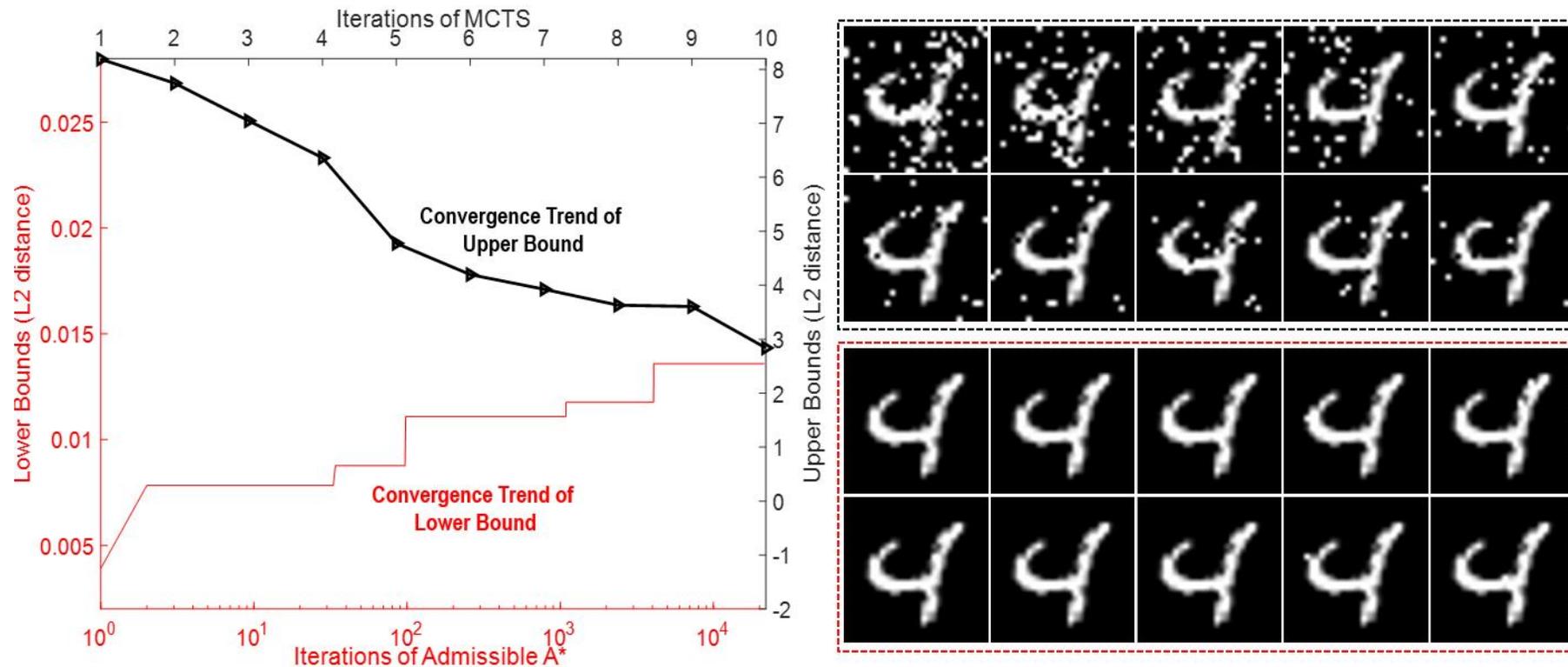
- **Goal** is finding adv. example, **reward** inverse of distance
- **Player 1** selects the **feature** that we will manipulate



- Each feature represents a possible move for player 1
- **Player 2** then selects the **pixels** in the feature to manipulate
- Use Monte Carlo tree search to explore the game tree, while querying the network to align features
- Method black/grey box, can approximate the **maximum safe radius** for a given input

# Guarantees for deep learning!

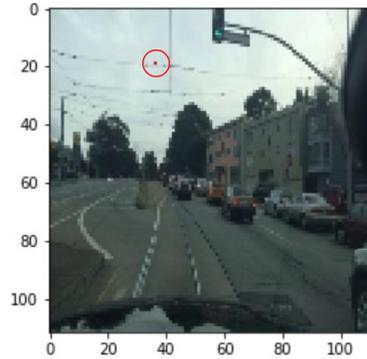
- Prove that **no** adversarial examples exist in a neighbourhood around an input
- Compute lower and upper bounds on **maximal safety radius**



[A Game-Based Approximate Verification of Deep Neural Networks with Provable Guarantees.](#) Wu *et al*, CoRR abs/1807.03571, 2018.

# Evaluating safety-critical scenarios: Nexar

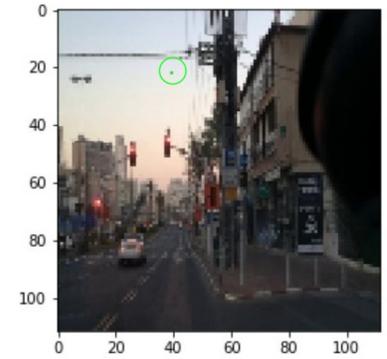
- Using our Game-based Monte Carlo Tree Search method we were able to **reduce the accuracy of the network from 95% to 0%**
- On average, each input took **less than a second** to manipulate (.304 seconds)
- On average each image was vulnerable to **3 pixel changes**



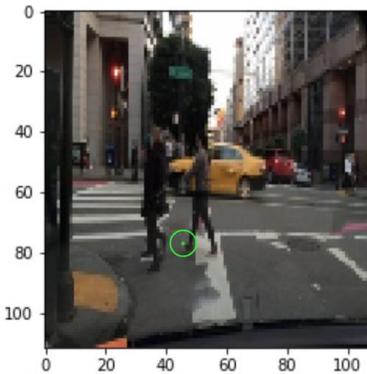
(a)



(b)



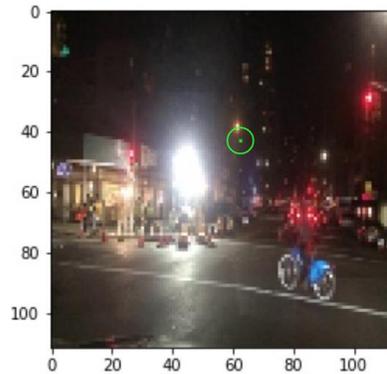
(c)



(a)

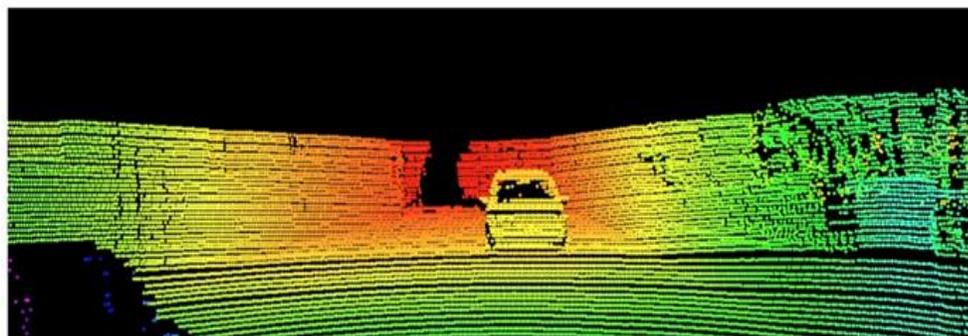


(b)



(c)

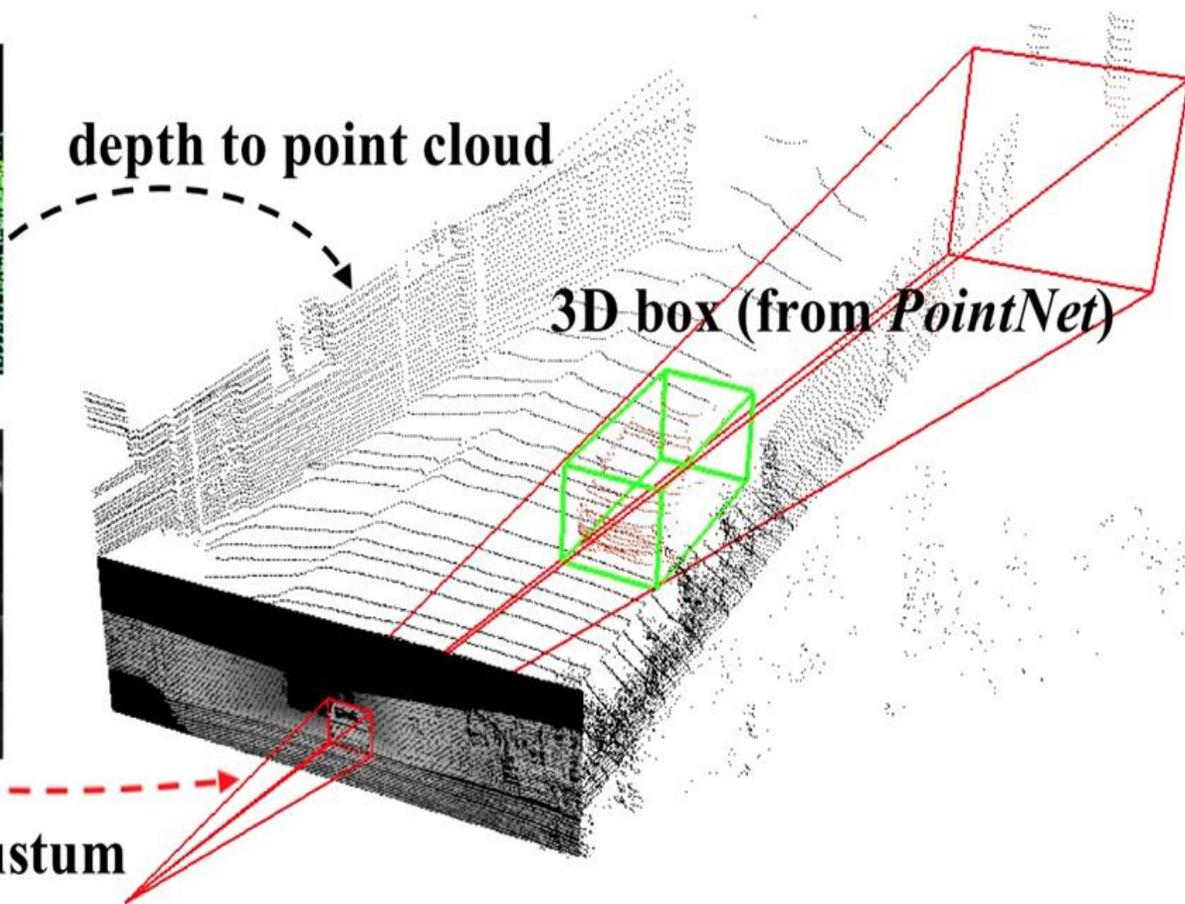
# 3D deep learning



depth to point cloud



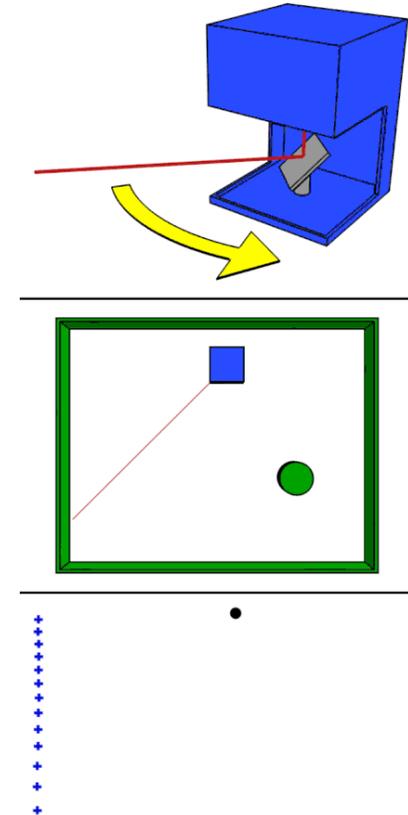
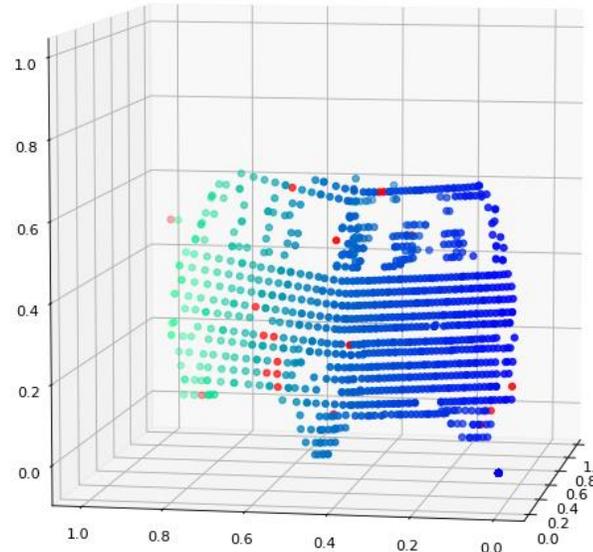
2D region (from CNN) to 3D frustum



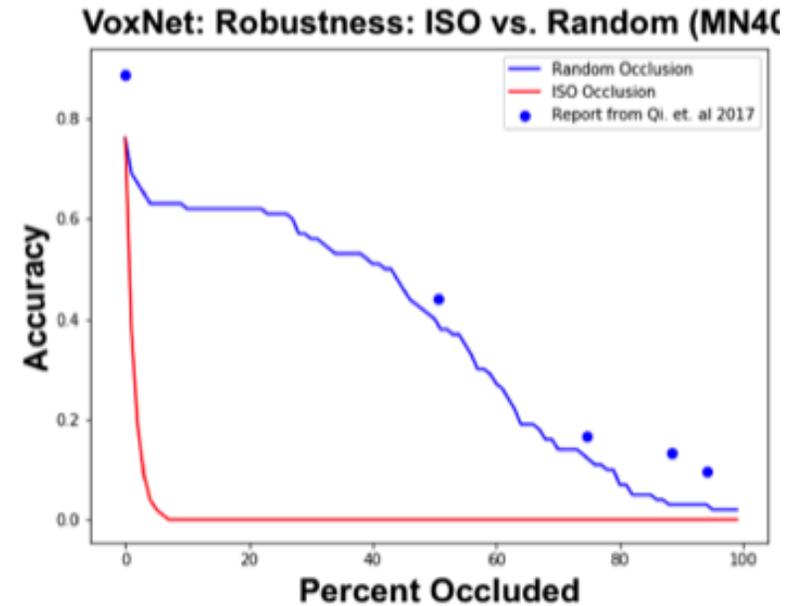
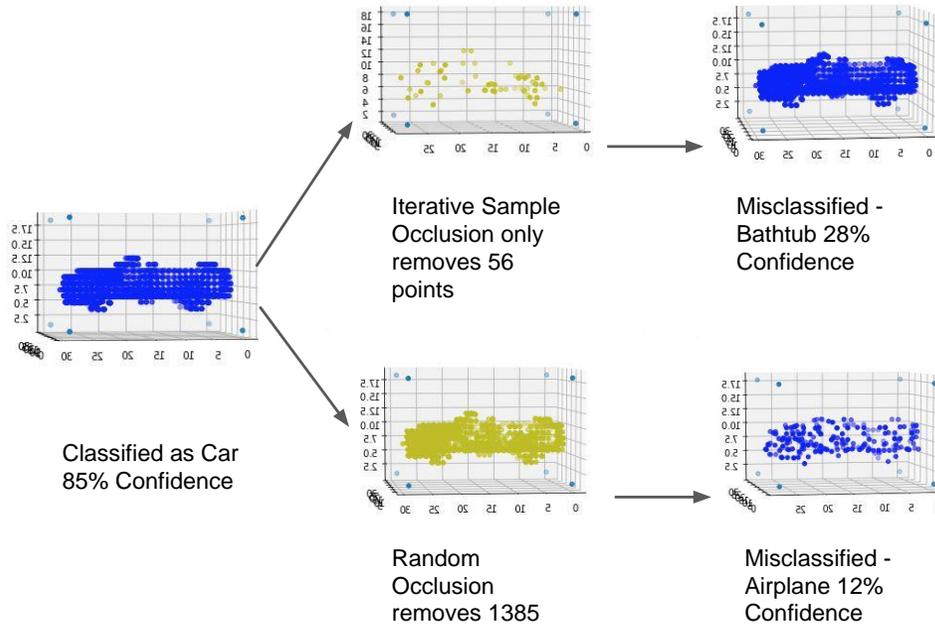
3D box (from *PointNet*)

# LiDAR and inherent error in point clouds

- Point ordering matters
- Partial occlusion of contiguous points
- Dark black could affect the reliability of sensor
- Misoriented sensors
- Need sub-second decision making



# Can also attack 3D deep learning (Lidar)



...reduce accuracy to 0% after occlusion of 6.5% of the occupied input space, targeting the critical set

# Probabilistic guarantees

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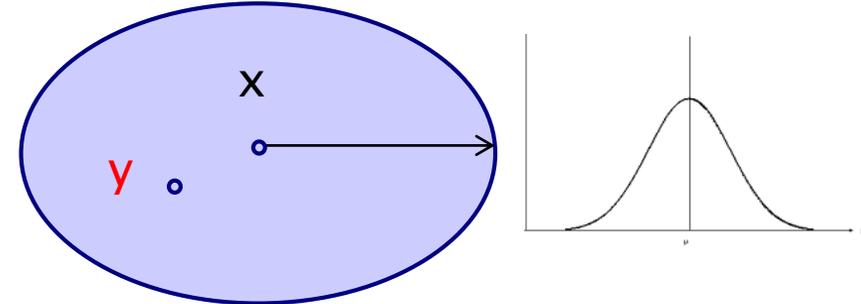
- Requiring that no adversarial examples exist too strict!
- Need to **probabilistic guarantees**: probability that local perturbations result in predictions that are close to original
- Taking account of the **learning** process
- Bayesian neural networks have **prior** on weights
  - account for noise, uncertainty, etc
  - return an uncertainty measure along with the output
- Need to compute posterior probability
  - often **intractable**
  - can we do better?

# Statistical robustness guarantees

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- Work with Bayesian neural networks

- Define **safety with prob**  $1 - \varepsilon$

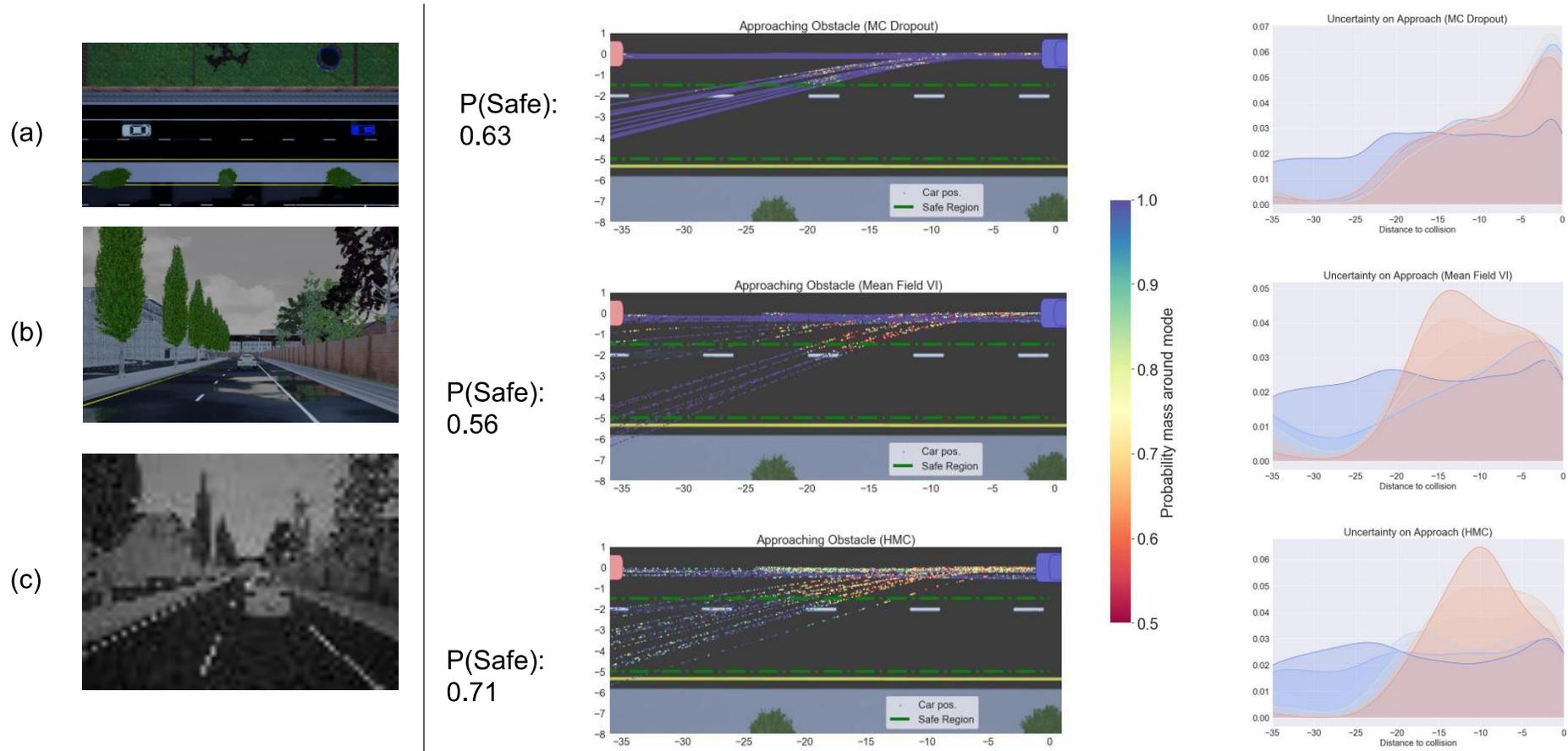


$$Prob(\exists y \in \eta \text{ s.t. } f(x) \neq f(y) \mid D) \leq \varepsilon$$

- i.e. **conditioned** on training data  $D$
- Method: **sample the weights**, then employ statistical model checking (Massart bounds, sequential test)
  - compare robustness and accuracy trade offs for different inference methods

# Uncertainty quantification with guarantees

- Safety verification for Bayesian neural network autonomous driving controllers



# But more progress needed...

## 'I hate them': Locals reportedly are frustrated with Alphabet's self-driving cars

- Alphabet's self-driving cars are said to be annoying their neighbors in Arizona, where Waymo has been testing its vehicles for the last year.
- More than a dozen locals told The Information they they hated the cars, which often struggle to cross a T-intersection near the company's office.
- The anecdotes highlight how challenging it is for self-driving cars, which are programmed to drive conservatively, to handle certain situations.

Published 3:04 PM ET Tue, 28 Aug 2018 | Updated 12:53 PM ET Wed, 29 Aug 2018



Source: Waymo

## Self-driving cars should be allowed to mount pavements and break speed limit in emergencies



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A Tesla Model S

# Concluding remarks

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- Much excitement about potential of the developments in AI
- and exciting opportunities!
  
- But deep learning should be more **critically evaluated** when put into practice in safety-critical situations
  
- We must have **guarantees** for safety, security, privacy, etc
  - formal verification, safety assurance
- and need to know **know the limits**, also for deep learning
  - rigorous foundations, methodology
- and **social implications**
  - ethics, fairness and morality
  
- Many challenges remain

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- New ERC Advanced Grant FUN2MODEL  
“From FUNction-based TO MOdel-based automated probabilistic reasoning for DEep Learning”
- Postdoctoral and PhD positions